## 14.2 Videos Guide

## 14.2a

- Definition of a limit of a function *f* of two variables
  - $\lim_{(x,y)\to(a,b)} f(x,y) = L \text{ if for every } \varepsilon > 0 \text{ there is a } \delta > 0 \text{ such that if } (x,y) \text{ is in the domain of } f \text{ and } 0 < \sqrt{(x-a)^2 + (y-b)^2} < \delta \text{ then } |f(x,y) L| < \varepsilon$

## Exercises:

14.2b

• Find the limit, if it exists, or show that the limit does not exist

$$\circ \lim_{(x,y)\to(2,-1)} \frac{x^2y + xy^2}{x^2 - y^2}$$
  
$$\circ \lim_{(x,y)\to(0,0)} \frac{5y^4 \cos^2 x}{x^4 + y^4}$$

14.2c

$$\circ \quad \lim_{(x,y)\to(0,0)} \frac{xy^4}{x^4 + y^4}$$

- Reminder of the Squeeze Theorem in  $\mathbb{R}^2$  (which also holds in higher dimensions)
  - If  $f(x) \le g(x) \le h(x)$  on an open interval containing a (except possibly at a) and if  $\lim_{x \to a} f(x) = \lim_{x \to a} h(x) = L$ , then  $\lim_{x \to a} g(x) = L$

Exercise:

- Determine the set of points at which the function is continuous.  $G(x, y) = \ln(1 + x - y)$
- Use polar coordinates to find the limit.  $\lim_{(x,y)\to(0,0)} (x^2 + y^2) \ln(x^2 + y^2)$